

# Constructing a Balanced, $\log(N)/\log\log(N)$ - Diameter Superpeer Topology

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# Outline

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- ∞ Superpeer Topologies
- ∞ Approximating Random Graphs
- ∞ Results and Comparison

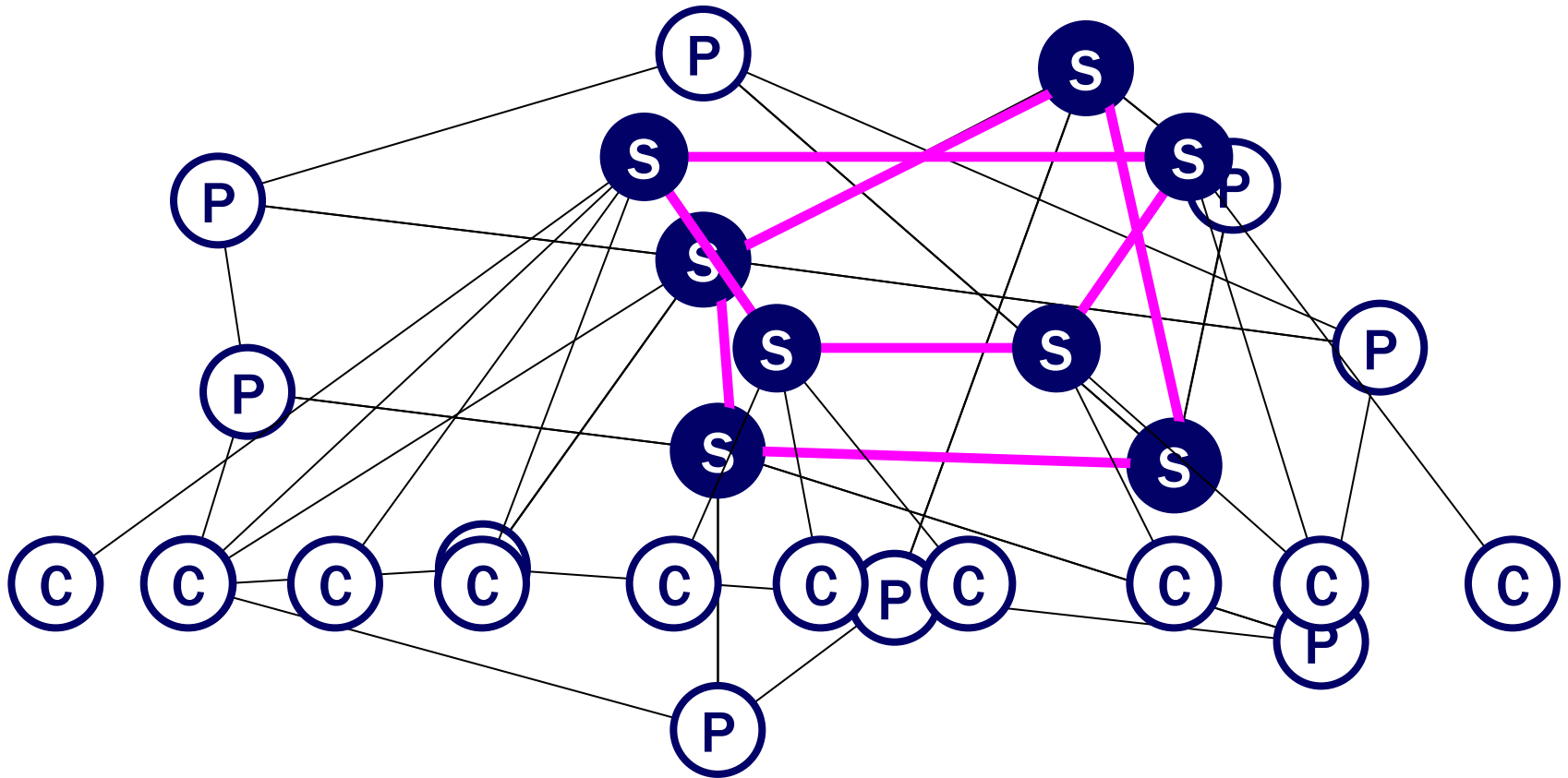
# Superpeers

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- ❧ Goal: improved scalability and performance for unstructured methods
- ❧ A two-level hierarchical P2P organization
  - ❧ upper level: super-peers
  - ❧ lower level: peers
- ❧ Queries are routed (via broadcasting) among super-peers only
- ❧ Proposed by KaZaA, adopted in Gnutella

# Example: Adding Superpeers

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# Superpeer Topology?

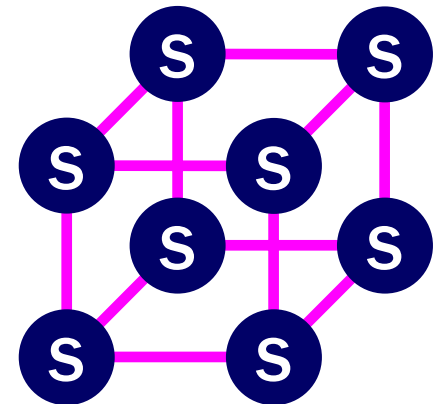
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## Desirable properties

- connected
- low diameter → fast search time
- low node degree → efficient
- regular → load balanced, avoid hot spots

## Example: the Binary Hypercube Topology

Problem: highly structured!



# Random Graphs

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∞ Erdős and Rényi, 1959

∞ The random graph process:

$G_0$  = the graph consisting of  $N$  vertices and no edges

for  $\tau = 1$  to  $N*(N-1)/2$  do

    select randomly an edge not in  $G_{\tau-1}$

    construct  $G_\tau$  by adding this edge to  $G_{\tau-1}$

# Properties of Random Graphs

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- ER-model random graphs are almost regular
- When the number of edges  $\tau = (N/2) \ln N$ , the graph suddenly becomes connected
  - at this point, average node degree =  $\ln N$
- Diameter  $D(G_\tau)$  at this *hitting time* =
$$\left\lceil \frac{\ln N - \ln 2}{\ln \ln N} \right\rceil + 1 \leq D(G_\tau) \leq \left\lceil \frac{\ln N + 6}{\ln \ln N} \right\rceil + 3$$
- Has desired properties, even though unstructured!

# Using Random Graphs for P2P?

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- ⌘ Problem: P2P systems are dynamic, not static
  - ⌘ i.e., nodes may join and leave
- ⌘ If edges are added equiprobably among all nodes, “older” nodes will have more edges than “younger” nodes



# Approximating Random Graphs

∞ Adding a vertex to graph  $G_t$  (with  $N$  vertices):

$$\delta = \lceil \ln(N) \rceil$$

while there are vertices with degree  $< \delta$

    select randomly a vertex  $u$  with degree less than  $\delta$

    connect  $u$  to a random vertex  $v$  of minimal degree

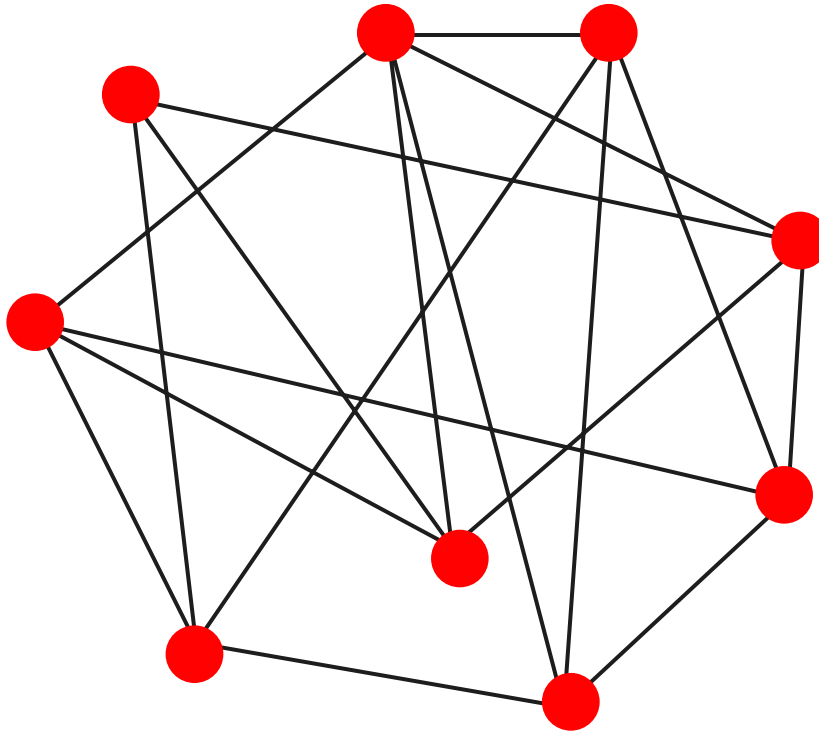
endwhile

return result as  $G_{t+1}$

∞ This is referred to as the  $\delta$ -process

# Approximation Example

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$$N = 9$$

$$\delta = 3$$

~~DONE~~

# SUPS: An Approximately Random Superpeer Topology

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- ⌘ Based on the Random  $\delta$ -Process
- ⌘ Fully distributed
  - ⌘ each node estimates the size of the network ( $N$ )
- ⌘ Designed to tolerate faults, and support high join / leave rates

# Information Needed by SUPS

Each node  $i$  maintains the following information

$N_i$	a local estimate of $N$
$\delta_i$	a local estimate of $\delta$
$d(i)$	$i$ 's current degree
$MinNode(i)$	a random lowest-degree non-neighbor
$MinList(i)$	sorted list of $\delta_j$ $MinNodes(i)$
$PriNodes(i)$	3 primary neighbors

Each node  $i$  periodically broadcasts  $i, N_i, d(i)$

“piggy-backed” onto query messages

# The Distributed $\delta$ -Process

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- Each node  $i$  independently executes the following when its estimate  $N_i$  changes

$$\delta_i = \lceil \ln(N_i) + 1 \rceil$$

while  $d(i) < \delta_i$

    select randomly a node  $v$  from  $MinList(i)$

    connect to  $v$

endwhile

# Joining the Superpeer Topology

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- ∞ A peer wishing to promote to a superpeer
  1. inherits the information maintained by its two “parent” superpeers
  2. invokes the distributed  $\delta$ -process
- ∞  $PriNodes(i)$  = first 3 nodes to which it connects
  - ∞ each of these 3 nodes broadcasts a  $Join(i)$  message
- ∞ A node  $j$  receiving 2 or more of these messages
  1. increments its value  $N_j$
  2. invokes the distributed  $\delta$ -process

# SUPS Resilience to Failures

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∞ Any value of  $N_i$  for which

$$\lceil \ln(N_i) + 1 \rceil = \lceil \ln(N) + 1 \rceil$$

will produce the correct estimate for  $\delta_i$

∞ i.e., there is a fairly large “noise margin” for estimation error

∞ When receiving a Join message, synchronize  $N_i$  with values from other nodes (on  $MinList(i)$ )

∞ Periodically tabulate (from scratch) the number of nodes  $N$  in the system, and broadcast  $N$

# Evaluation of SUPS

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## ∞ Simulated just the graph construction

- ∞ since queries are broadcast, there is no need to simulate them

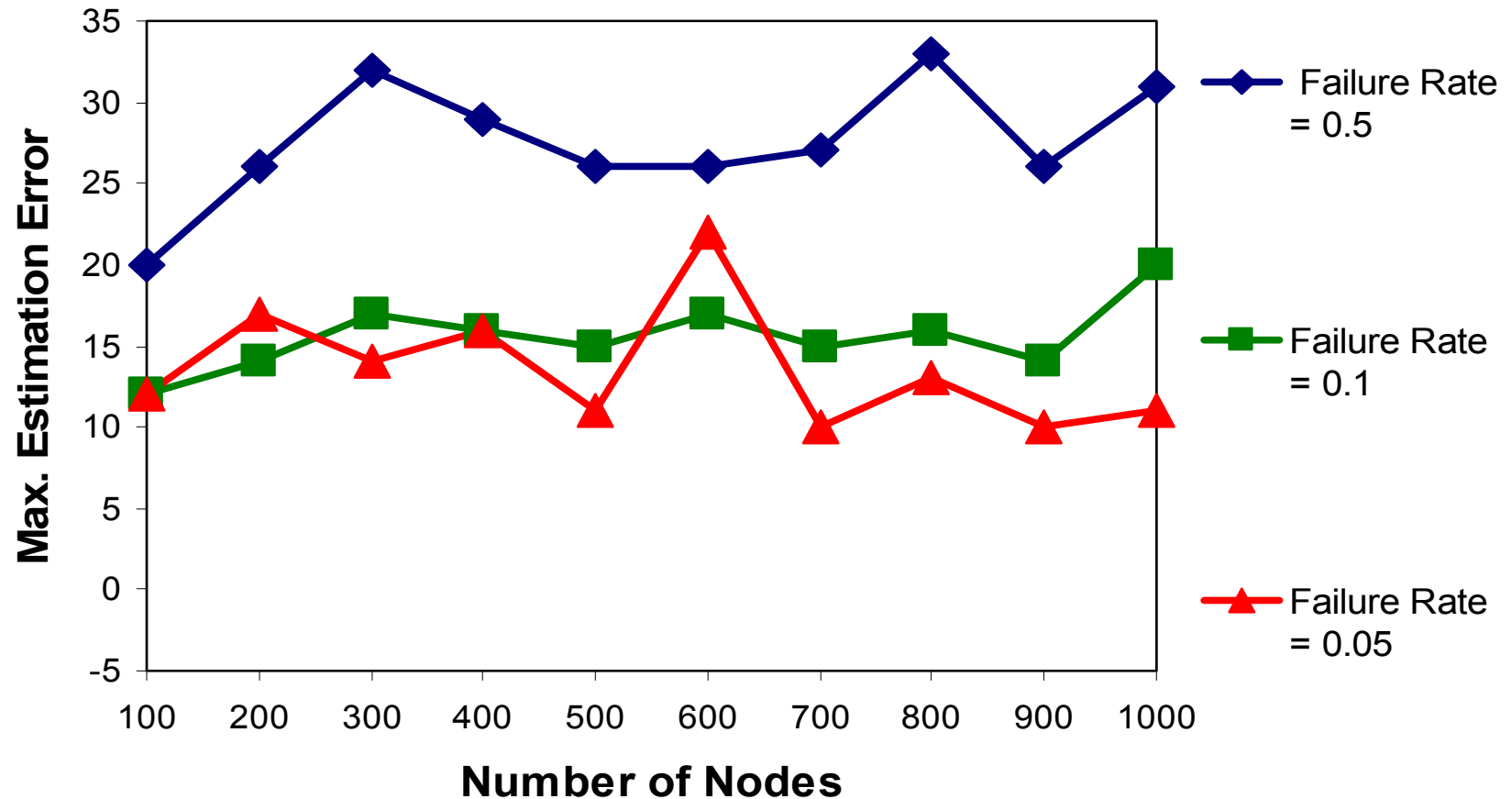
## ∞ Measurements

- ∞ impact of failures on the accuracy of  $N_i$  and  $\delta_i$
- ∞ diameter of network
- ∞ node degree
- ∞ (fraction of nodes affected by a node join or leave)

## ∞ Resulting graphs always connected

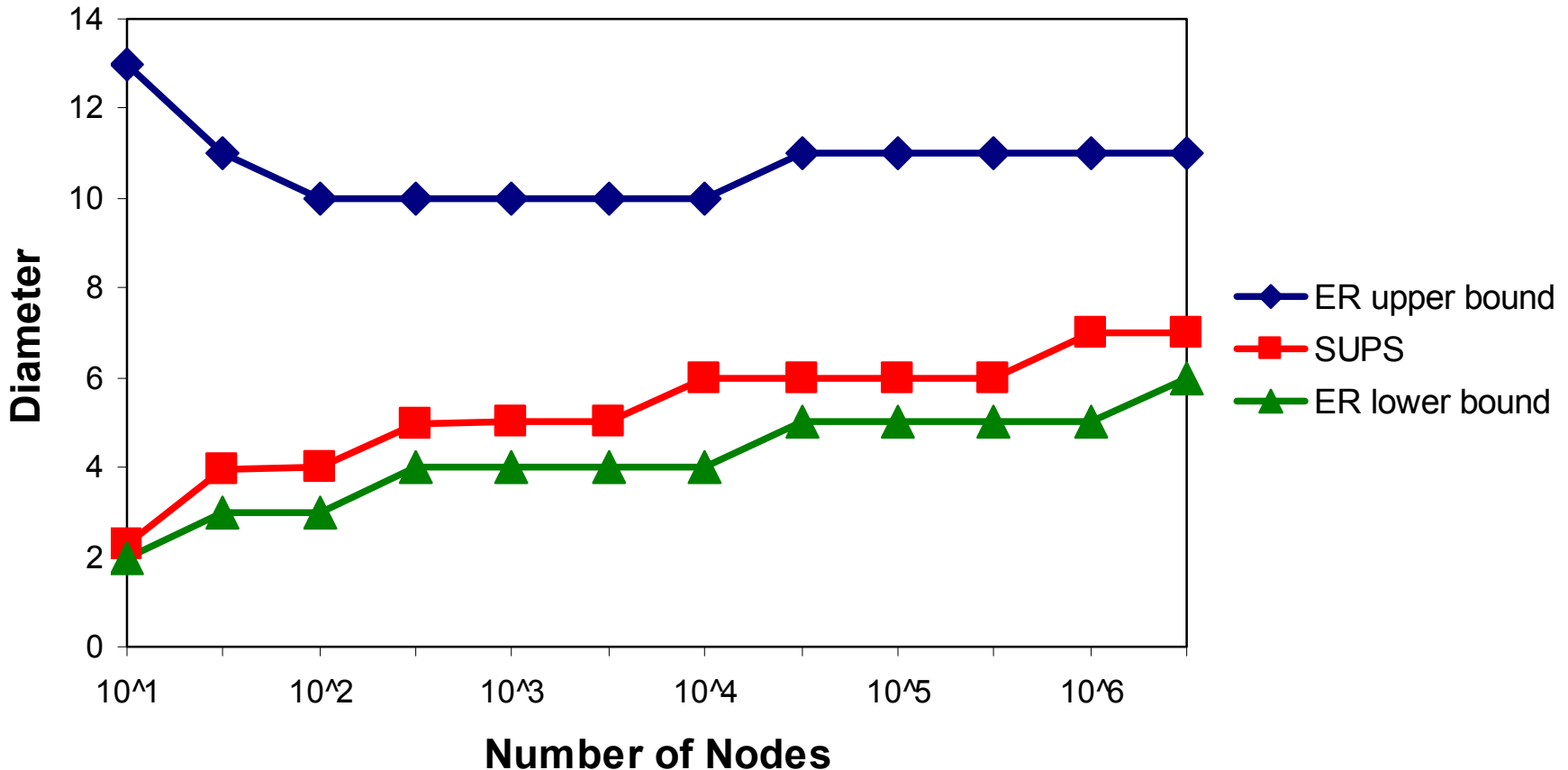


# Results: Error in Estimating $N$



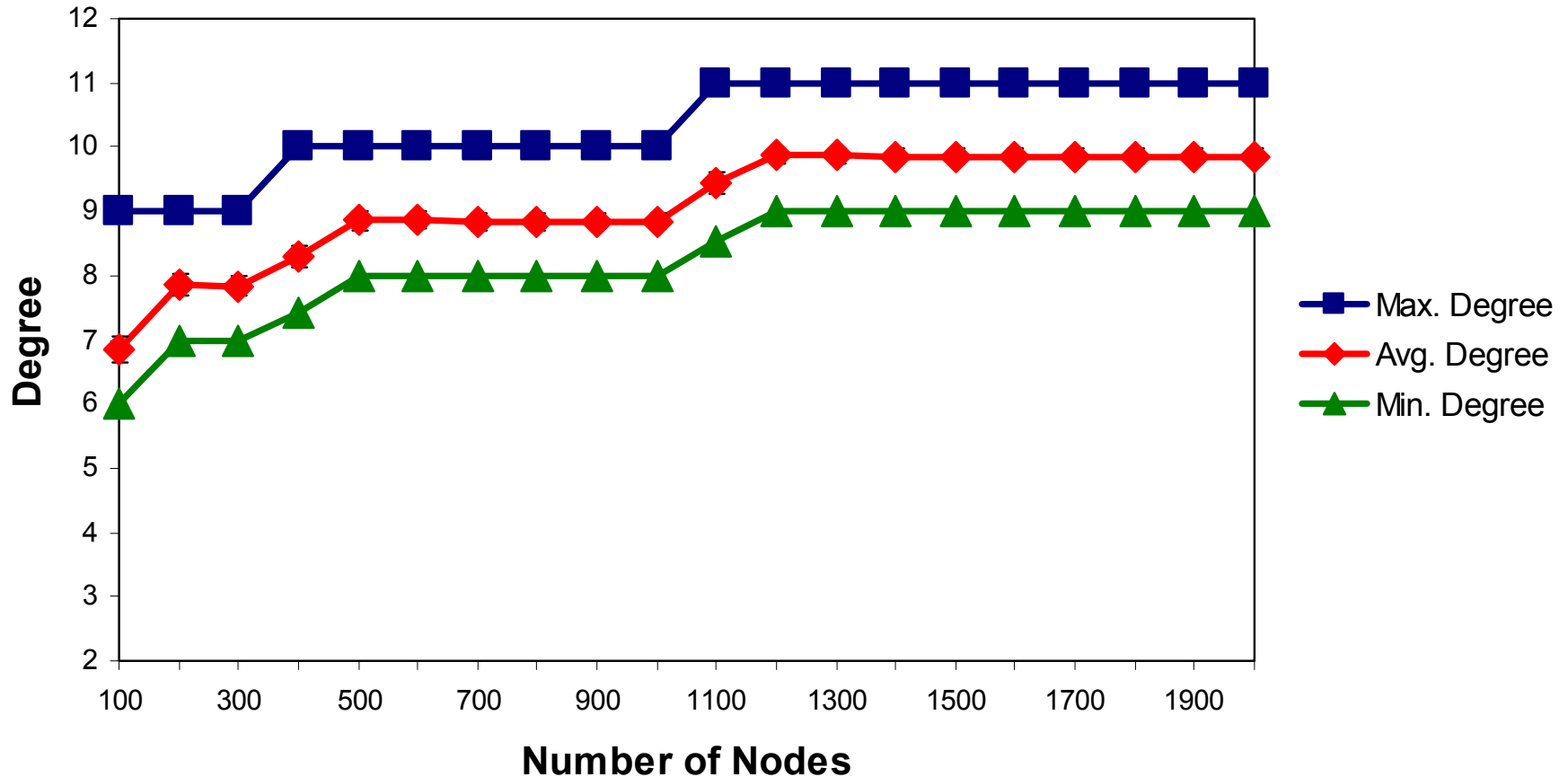
→ Error in estimating  $\delta$  always  $\leq 1$

# Results: Diameter



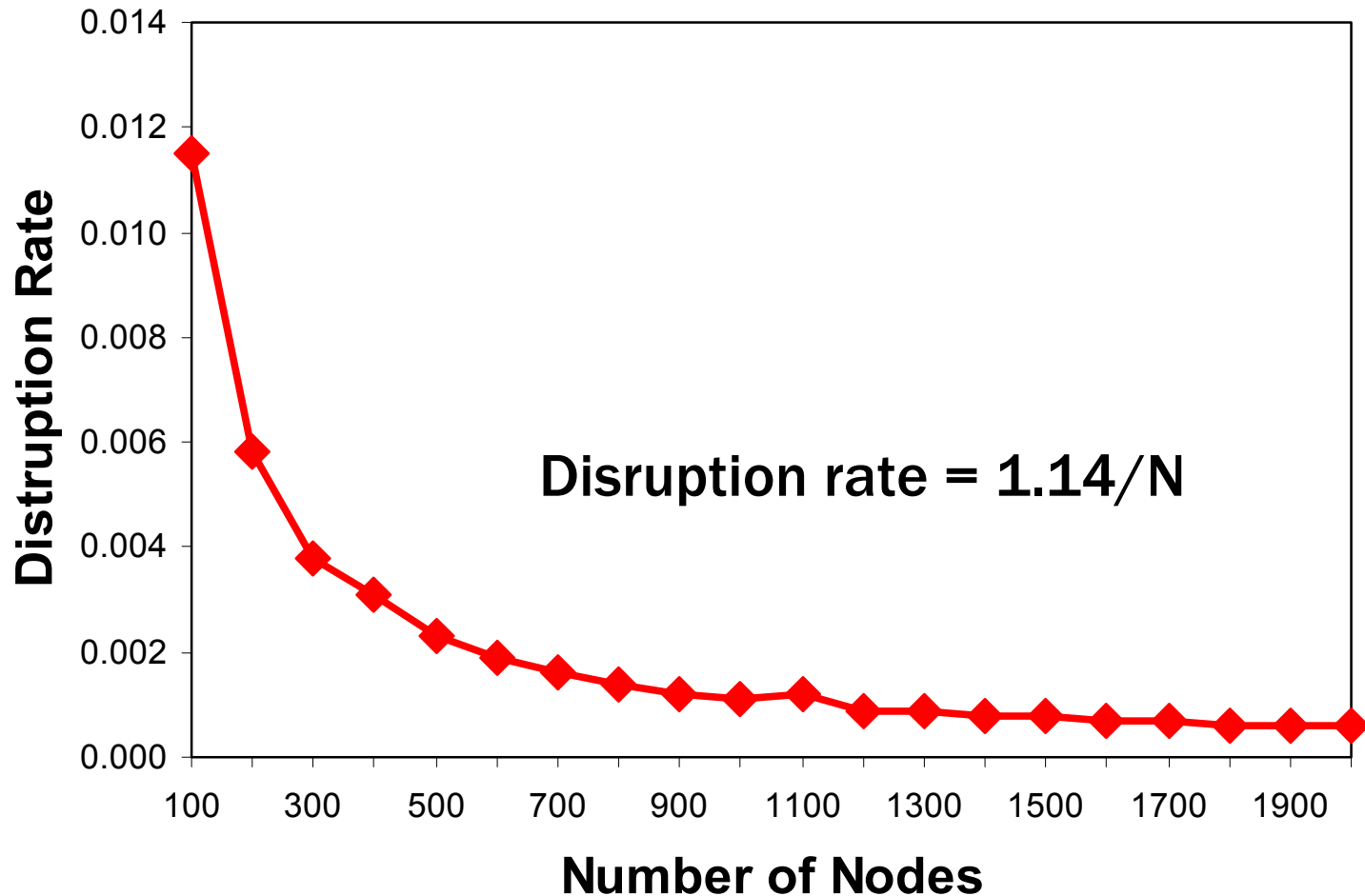
➔ Diameter of SUPS close to ER model lower bound

# Results: Node Degree / Regularity



➔ SUPS produces an almost  $\theta(\ln N)$ -regular graph

# (Results: Disruption Rate)



⌘ Avg. of 1.14 nodes are affected regardless of N

# Comparison with Gnutella v0.6

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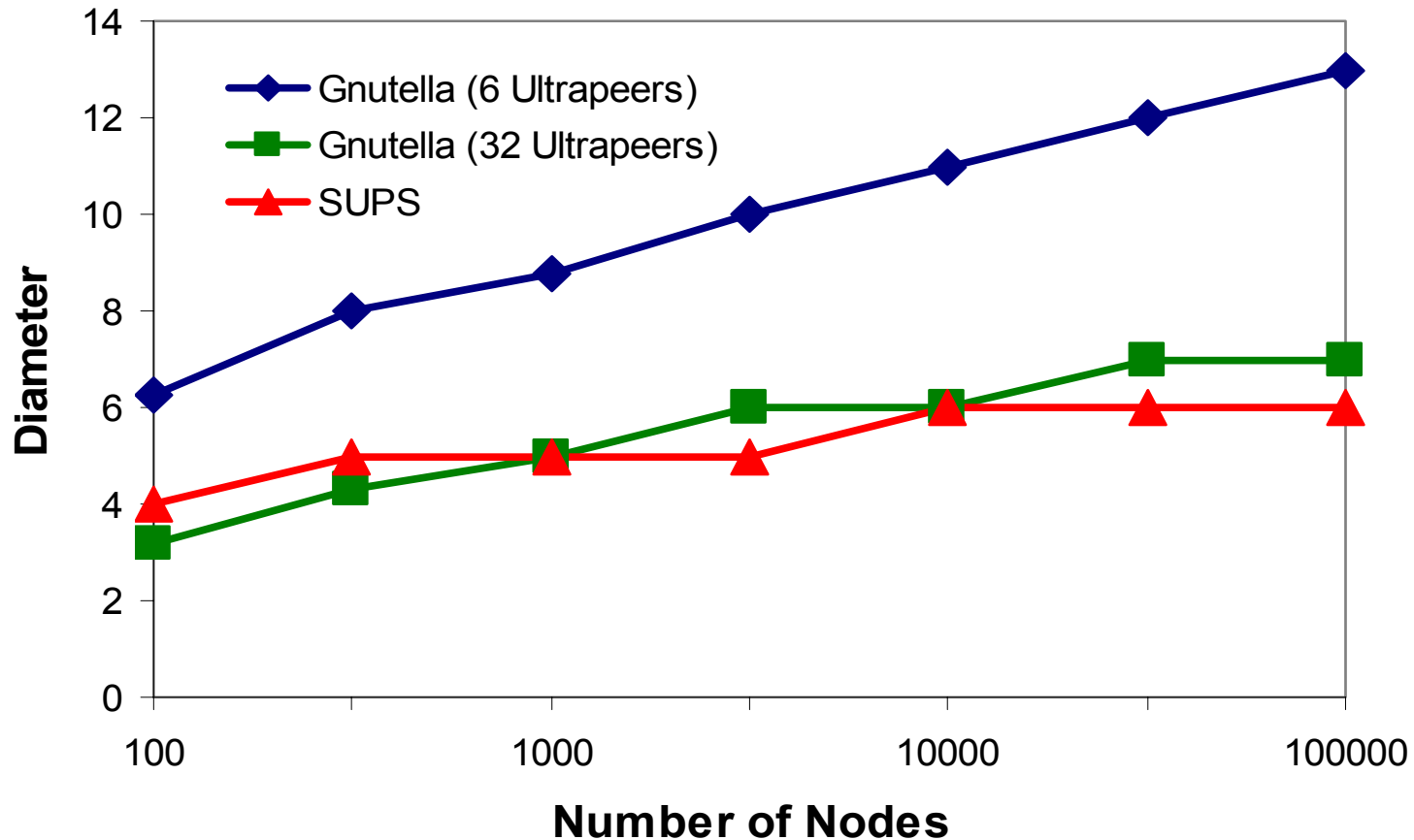
## ☞ Gnutella has proposed *ultrapeers*

- ☞ degree of each ultra peer = 6 (earlier) or 32 (more recently)
- ☞ we generated connections perfectly randomly (unrealistically favorable)

## ☞ Measurements

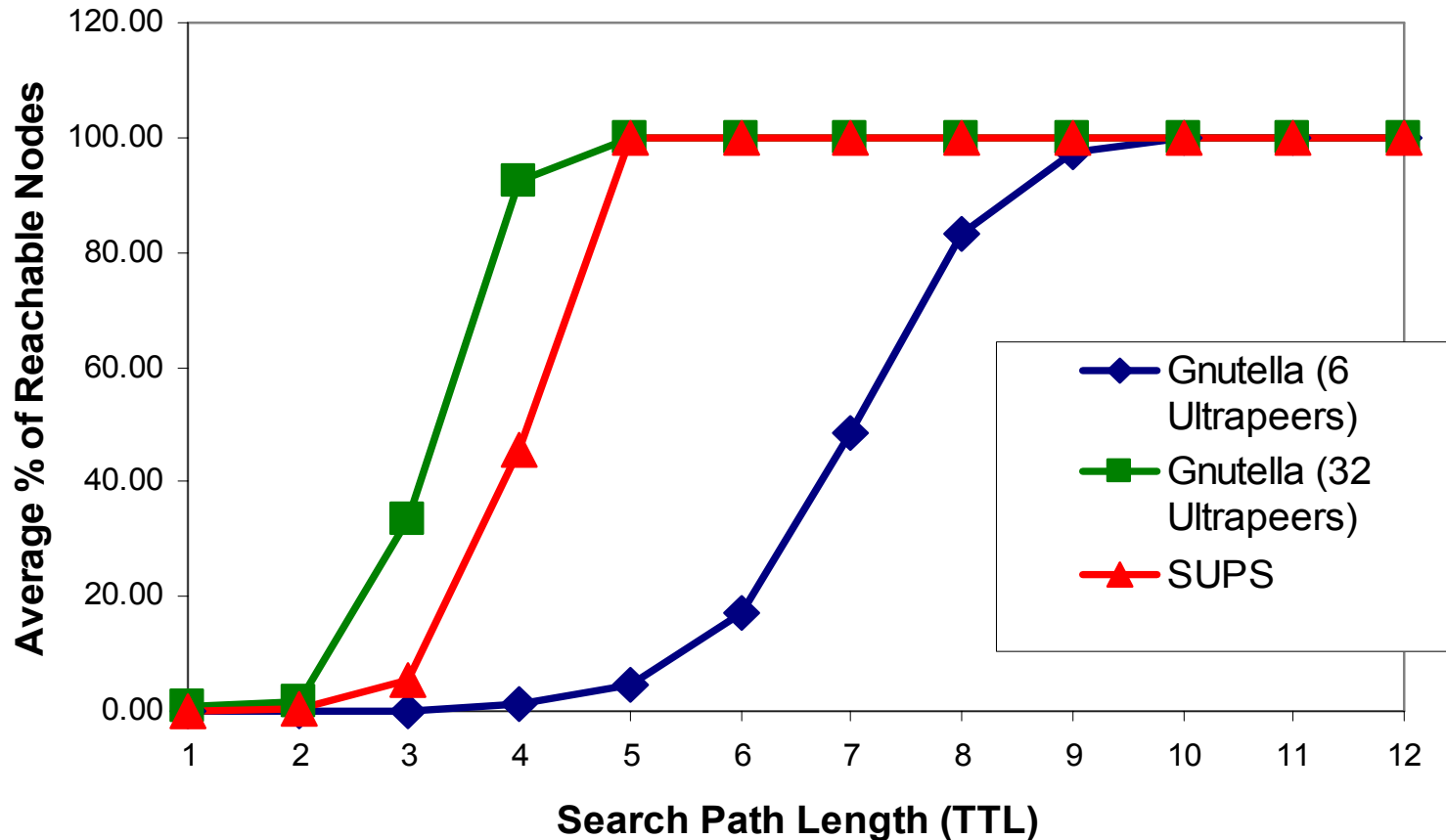
- ☞ diameter
- ☞ reachability = fraction of nodes reachable within a given TTL

# Comparison: Diameter



- ➔ G32 : same diameter (w. 190% more edges)
- ➔ G6: 83% bigger diameter (w. 45% fewer edges)

# Comparison: Reachability



- ➔ G32 : equivalent reachability in 1 less “hop”
- ➔ G6 : much worse reachability

# Conclusions

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- ❧ Random graphs are a very good unstructured topology for P2P
- ❧ SUPS produces a good approximation of a random graph
  - ❧ low overhead, simple, and practical
  - ❧ robust to failures and rapid changes of nodes
  - ❧ compatible with currently-deployed P2P systems
- ❧ Suitability of the  $\delta$ -process for other distributed applications?